

2018

SEMESTER 2

363 Rotor Design Report

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1 Summary

1.1 Rotor Purpose

The rotor is a commercial product. The target market is rural communities in the higher windy latitudes around the world. The product will consist of a kitset used to build a general assembly, a fixture on a locally constructed tower. See 1. for rotor application and kitset components. The kitset will include instructions for assembly.

1.2 Achievement of Purpose

Our chosen design of six blades with fifteen sd7003 aerofoils per blade will: meet the design criteria (below), be easy to both distribute to and assemble by rural communities using the compact kitset, and contain key components and samples of easily assessable surfacing and adhesive materials. The surfacing materials are duct tape, sellotape and hot glue.

1.3 Design Criteria

The rotor must operate in wind conditions between eight to twelve knots, rotating at 140 rpm at the target windspeed of ten knots. The rotor must have between three to eight blades. The general assembly must be easy to assemble from the kitset using the instruction manual. Blade surfacing and adhesives must be easy for rural communities to source for repairs and maintenance. The rotors components and materials must have the strength and durability to withstand the operating environment and are of low cost for maintenance and repair.

1.4 Analysis

The analysis was broken up into a series of discrete steps: Understanding the fundamental rotor theory. Writing an Iterative scheme in MATLAB. Conducting complete enumeration with every aerofoil design. Ruling out a series of aerofoil designs in a stage one selection process. Iterating on selected aerofoil designs, changing the number of blades and sections. Selecting the number of blades and aerofoils in a stage two selection process. Making manufacturing considerations in the design. Making the final selection based on the all major factors. Considering surfacing materials.

The main factors considered in the design are: The lift to drag (CL/CD) ratios for the aerofoil design across a range of angles of attack (α) and different windspeeds expressed by different Reynolds numbers. The margin of error in CL/CD ratios with changes in the angle of attack and windspeed, assessed in the CL/CD vs α plots for every aerofoil. The thickness of the aerofoil. The camber of the aerofoil. The shape of the aerofoil. The surface area of the aerofoils. The cost, manufacturability and durability of surfacing materials.

1000 different aerofoil designs were investigated in complete enumeration. After, 37 aerofoil designs were considered for stage two. In stage two, 333 different combinations were considered, the 37 selected aerofoils from stage one with 4,5 or 6 blades and 14,15 or 16 sections. 37 from stage two were considered to make the final selection. 1259 unique designs were considered in the process.

1.5 Conclusion

Our final design is a rotor with six blades with fifteen sections per blade. Each section is a sd7003 aerofoil design with varying chord lengths between 28.3 and 19.5cm, and a total blade length of 69.0cm from the

centre of the hub. Each aerofoil has a camber of 1.2% of chord length. Each aerofoil has a different blade setting angle in the range of 28.6 to 13.0 degrees. The aerofoils are equally spaced along the blades, starting at 26cm from the centre of the hub and ending at 69.0cm. The aerofoils are surfaced using sellotape, duct tape and hot glue. See 2 for exact parameters and dimensions.

The design was the best of the last 37 in the final selection stage, maximising the Cl/Cd ratios whilst having the most reasonable margin of error with changing angles of attack and windspeeds. The aerofoil had a smooth, continuous shape with slight camber, easy to laser cut and surface. Each aerofoil was thick enough to insert the blade rods. The weight per blade is low considering the number of sections, aerofoil surface area and thickness of the acrylic. Six blades decreased the chord lengths and increased our margin of error for manufacturing faults. Fifteen sections maximised the Cl/Cd ratios compared to other combinations. Sellotape and duct tape are durable, easy to apply and inexpensive compared to other materials. The hot glue is easy to apply and inexpensive compared to other adhesives.

1.6 Cost

The total rotor, two blade setting rigs and one extra blade will cost \$241.79. See 3 for a full cost breakdown.

1.7 Performance

Our turbine will achieve 47.6W with a torque of 3.25m across all three windspeeds with 140rpm. The turbine will generate a power coefficients of 0.3978, 0.3632 and 0.3064 at 8,10 and 12 knots respectively.

2 Development of Design

2.1 Assumptions

We made the following assumptions to conduct our analysis: Fundamental rotor theory is applicable and does not break down. Assume losses due to wake rotation, aerodynamic drag, tip losses and losses attributable to having a finite number of blades. The mechanic system the rotor spins on is 100% efficient. Wind direction is perpendicular to the rotor and flows in one dimension.

2.2 Drawings

See 4.4 for drawings on the aerofoil design and the blade distance setting tool used in construction.

2.3 Method of Analysis

See 4 for our nine-stage method of analysis.

(1) Fundamental Rotor Theory. We learnt extracting power from the wind using a rotor. We learnt the following concepts: Lift and drag around an aerofoil design and deriving their subsequent coefficients. Learning how to extract power from the wind considering the Betz Limit, Bernoulli Analysis, axial induction factors, pressures, velocities and forces. The limitations of rotor design. The blade element momentum method considering both axial and angular induction factors. Incorporating axial induction factors and taking into consideration wake rotation and Prandtl tip loss. See 5 for lectures slide three through to eight where the aforementioned theory was covered.

(2) An iterative scheme. XfoilIteration.m was devised using the fundamental theory in MATLAB. The names of the aerofoil designs were extracted from an aerofoil bank. The aerofoil names were passed into evaluatePlot.m to generate CL/CD plots across a range of alphas and Reynolds numbers. The CL, CD and alpha values were found by using the callXfoil.m and Xfoil.m scripts, written by Kevin Jia. The plots were saved in a directory. The fundamental theory calculations were written in evaluateTurbine.m, returning the following parameters: Power coefficient of rotor power over system power, number of blades and sections, windspeed, angle of attack, Reynolds number, radii for aerofoil locations, chord lengths and the blade setting angles. These parameters were stored in an excel spreadsheet. See 5.1 for aforementioned MATLAB scripts.

(3) Complete Enumeration. The iterative scheme was applied to approximately 1000 aerofoil types, focusing on the CL/CD vs Alpha plots for a range of Reynolds numbers. These plots were stored in a directory. See 5 for a subset of plots.

(4) Stage One Selection. Each plot was accessed on the CL/CD magnitude and margin of error for changing alphas and Reynolds numbers. An ideal plot was one with a high CL/CD ratio with flat curves and tight bands, a similar shape to a rainbow. This stage eliminated 963 designs, leaving 37 as listed in 6.

(5) Blade and Section Iteration. The number of blades and sections varied in another implementation of the iterative scheme. After investigating combinations of blades (four, five or six) and sections (fourteen, fifteen or sixteen). These results were stored in an excel spreadsheet. See 7 for one third of total iterations.

(6) Stage Two Selection. After reviewing the spreadsheet, six blades with fifteen sections gave the best CL/CD ratios with adequate chord lengths for the 37 aerofoils considering manufacturing errors and blade redundancy.

(7) Manufacturing Considerations. The 37 aerofoil designs were assessed on four factors: their plot from stage one selection, their shape looking at the profile on airfoiltools.com, their camber, and their thickness calculated from a percentage of chord length. The plots were ranked amongst themselves between 0 (low) to 3 (high). The shape had to be smooth and continuous for easy laser cutting. The foil design must have some camber and have a low surface area. The minimum thickness of the aerofoil must be as greater than 14mm to allow a 10mm diameter rod insert with 2mm spacing to the edge either side. See 8 for the evaluation.

(8) Final Selection. After considering the aforementioned factors in the manufacturing considerations, sd7003 with 6 blades and 15 aerofoils was the chosen design. See 9 for a profile and plot of this design.

(9) The materials used must be strong enough to withstand the applied operating loads to meet the target of 140 rpm. The acrylic (PMMA) aerofoils and aluminium hubs/rods/hub-rod inserts are strong enough to withstand those loads and easy to manufacture. The blade surfacing material must be lightweight, smooth and easy to apply to create a smooth surface on the aerofoil design. Achieving these criteria leads to maximising the lift to drag ratios, maximising the power extracted from the wind, and therefore meeting the objectives outlined in the design criteria. After considering materials, sellotape on the blade surfaces with duct tape on the sides for strength were chosen. These will minimise weight, be strong enough to withstand the operating environment, and are easy to apply and source. Other materials such as shrink wrap are difficult to apply and source, not suitable for the repair and maintenance in rural communities. Hot glue is a suitable yet cost effective adhesive with adequate strength to fix the aerofoils to the rods.

3 Design Calculations

3.1 Final Input Parameters

$V_u (m s^{-1})$	5.14	RPM ($\frac{r}{min}$)	140	Hub Radius (m)	0.26	C_p	0.3632	C_L	0.7202
$\rho, air (kg m^{-3})$	1.29	Torque (Nm)	3.25	# of Blades	6	P_s (W)	47.6475	C_D	0.0218
η_{system}	1	# of sections	15	Re	60,000	α	0.0873		

3.2 Blade Chords and Angles

Calculate the blade radius (R). R needs to be divided into the number of sections starting from the hub radius (0.26m) until the end (0.6896m). I will use one aerofoil section (The hub radius, $r = 0.26m$) to demonstrate. The calculations account for Prandtl tip loss and wake rotation. When starting the iterative scheme, begin with the betz limit ($C_p = 0.593$). C_p will update on subsequent iterations until the tolerance criteria is met.

$$\text{Rotor Radius: } R = \sqrt{\frac{2P_s}{C_p \eta \rho \pi V_u^3}} = \sqrt{\frac{2 \times 47.6475}{0.3632 \times 1 \times 1.29 \pi \times 5.1444^3}} = 0.6896m$$

$$\text{Tip speed ratio: } \lambda_r = \frac{\Omega r}{V_u} = \frac{2 \times 140 \times \pi \times 60^{-1} \times 0.26}{5.1444} = 0.7410$$

$$\text{Local wind angle: } \phi = \frac{2}{3} \tan^{-1}\left(\frac{1}{\lambda_r}\right) = \frac{2}{3} \tan^{-1}\left(\frac{1}{0.7410}\right) = 0.6221 \text{ rad}$$

$$\text{Chord length with Wake Rotation: } c = \frac{8\pi r}{BC_L} (1 - \cos\Phi) = \frac{8\pi \times 0.26}{6 \times 0.7202} (1 - \cos(0.6221)) = 0.2833m$$

$$\text{Blade Setting Angle: } \beta = \frac{180}{\pi} \times (0.6221 - 0.0873) = 30.6420 \text{ degrees}$$

Repeating this process for all other radii in the final design, the blade chord and angles are as follows.

Radii (m)	0.26	0.2907	0.3214	0.3520	0.3827	0.4134	0.4441	0.4748
Chord length (m)	0.2832	0.2821	0.2785	0.2732	0.2667	0.2598	0.2524	0.2449
Blade Setting Angle (Degrees)	30.64	28.57	26.68	24.94	23.34	21.88	20.54	19.31
Radii (m)	0.5055	0.5361	0.5668	0.5975	0.6282	0.6589	0.6896	
Chord length (m)	0.2373	0.2298	0.2226	0.2155	0.2088	0.2021	0.1959	
Blade Setting Angle (Degrees)	18.17	17.14	16.17	15.28	14.46	13.69	12.98	

3.3 Rotor Torque and Co-efficient of Power

Coefficients ($r=0.26m$): $C_n = C_L \cos(\phi) + C_D \sin(\phi) = 0.5980$ and $C_t = C_L \sin(\phi) - C_D \cos(\phi) = 0.4019$

$$\text{Factors: } F = \frac{2}{\pi} \cos^{-1}(e^{-f}) \text{ where } f = \frac{B(R-r)}{2r \sin(\phi)} = \frac{6 \times (0.6896 - 0.26)}{2 \times 0.26 \sin(0.6221)} = 8.5059$$

$$\text{Factors: } F = \frac{2}{\pi} \cos^{-1}(e^{-8.5059}) = 0.9999$$

$$\text{Blade Solidarity: } \sigma' = \frac{Bc}{2\pi r} = \frac{6 \times 0.2832}{2\pi \times 0.26} = 1.0404$$

$$\text{Axial Induction Factor: } a = \frac{\sigma' C_n}{4F \sin^2(\phi) + \sigma' C_n} = \frac{1.0404 \times 0.5980}{4 \times 0.9999 \sin^2(0.6221) + 1.0404 \times 0.5980} = 0.3142$$

$$\text{Tangential load: } \frac{1}{2} \rho \frac{V_u^2 (1-a)^2}{\sin^2(\phi)} C_t c = \frac{1}{2} \times 1.29 \frac{5.1444^2 (1-0.3142)^2}{\sin^2(0.6221)} \times 0.4019 \times 0.2832 = 2.6920N$$

$$\text{Incremental Torque: } \Delta Q_{i,i+1} = \int_{r_i}^{r_{i+1}} P_T r dr = \int_{r_i}^{r_{i+1}} P_T r dr = \int_{0.26}^{0.2907} 2.6920 r dr = 0.0228 Nm$$

Need the torque from all sections. Repeat with the remaining sections and sum to get $Q = 3.250$ as required.

$$\text{Power extracted: } P_E = Q \times \Omega = 3.250 \times 2 \times 140 \times \pi \times 60^{-1} = 47.6475$$

$$\text{Power available: } P_T = \frac{1}{2} \rho \pi R^2 V_u^3 = \frac{1}{2} \times 1.29 \pi \times 0.6896^2 \times 5.1444^3 = 131.1796$$

$$\text{Power Coefficient: } C_p = \frac{P_E}{P_T} = \frac{47.6475}{131.1796} = 0.3632 \text{ as required.}$$

4 Appendices

4.1 Background and Product Requirements

Project Description

Background and Product Requirements

WindPac, a New Zealand producer of wind turbines would like to develop a product for sale to remote communities in the higher windy latitudes of the South Pacific and the World (remote Africa, South America etc.).

The product will consist of:

1. A generator assembly that will fit onto a locally constructed turbine tower.
2. A rotor kitset consisting of pre-cut rotor blade profiles that insert into rods, a hub for inserting the rods into, materials for covering the blades, gauges and jigs for correct assembly of the blade profiles onto the rods.

WindPac wants a prototype rotor and a mock-up of the rotor kitset. The kitset will consist of:

- a) The parts required for the rotor blades;
- b) Jigs and fixtures for correct assembly;
- c) Instructions for assembly.

Rotor design specifications are set down below:

Air speed	8 – 12 knots, with a target at 10 knots
Torque-speed curve	Refer to Figure 1
Number of blades	3 to 8
Preferred turbine speed at 10 knots	~140 rpm

In your project groups, you will design, build, test and report on the construction of your prototype.

Project groups will be announced on **Friday 27 July**.

Figure 1: Background and Product Requirements in the Project Brief

4.2 Final Design Dimensions

Name	sd7003.dat
Number of Blades	6
Number of Sections	15
Windspeed (m/s)	5.1444
Alpha (rad)	0.087266
Reynold's Number	60000
Plot	3
Thickness	8.5%
Camber	1.2%
Shape	3
Minimum Thickness (mm)	16.65

Section	1	2	3	4	5	6	7	8
Radii (m)	0.26	0.290683	0.321367	0.35205	0.382733	0.413417	0.4441	0.474783
Chordlength (m)	0.283274403	0.282054	0.278453	0.273203	0.266861	0.259838	0.252436	0.244874
Blade Setting Angle (Degrees)	30.6420011	28.57435	26.67673	24.93728	23.34338	21.8824	20.54216	19.31121
Section	9	10	11	12	13	14	15	
Radii (m)	0.505466617	0.53615	0.566833	0.597517	0.6282	0.658883	0.689567	
Chordlength (m)	0.237306432	0.229841	0.222551	0.215485	0.208672	0.202128	0.19586	
Blade Setting Angle (Degrees)	18.17896164	17.13578	16.17293	15.28259	14.45771	13.69203	12.97994	

Figure 2: Exact Dimensions for the Final Design

4.3 Costs

Item	Cost/Unit (\$)	Cost/Length (\$/M)	# of Units	Length/blade (m)	# of Blades	Cost (\$)	Notes
Hub	150	#N/A	1	#N/A	#N/A	150	Only one hub
Aluminium rods	#N/A	3.20	#N/A	0.648	7	2.07	Includes an extra rod for one extra aerofoil blade. The rod doesn't go to the centre so is slightly shorter than the blade length. The rod length is blade length - hub radius (50mm) + rod connector hub insert length (8mm)
Acrylic sheets (PMMA)	6.36	#N/A	3	#N/A		19.08	Includes two blade setting rigs and an extra set of aerofoils for one extra blade.
Rod-Hub connection fitting	5.71	#N/A	7	#N/A		39.97	Includes an extra connector for a spare blade.
Cellotape	4.35	#N/A	3	#N/A		13.05	Two and a half blades per roll.
Duct Tape	10.89	#N/A	1	#N/A		10.89	For the blade edges
Hot Glue	6.73		1	#N/A		6.73	One for gluing all blades.
Total						241.79	Total cost for rotor + one spare blade and two blade setting rigs for the kitset.

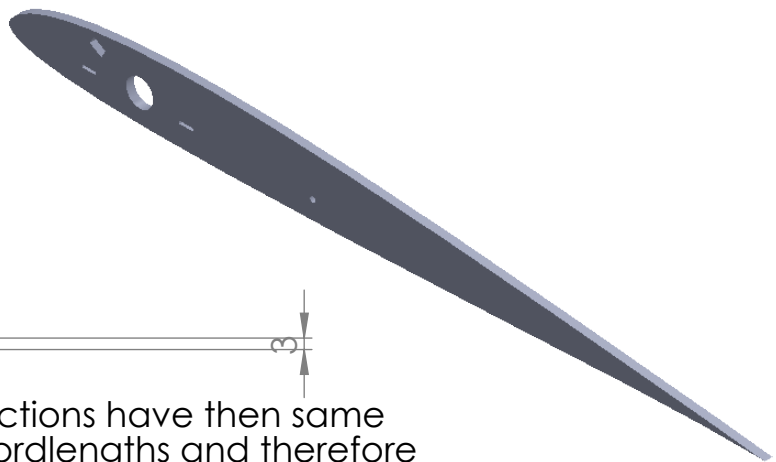
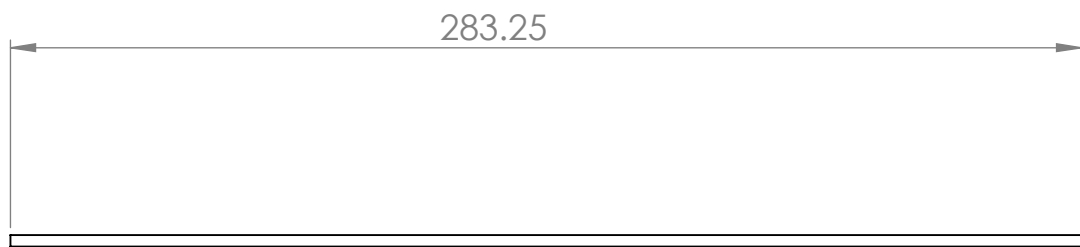
Figure 3: Costs for the Final Design including Two Blade Setting rigs and One Spare Blade

4.4 Models and Drawings : Parts, Rigs and Assemblies

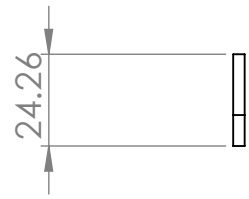
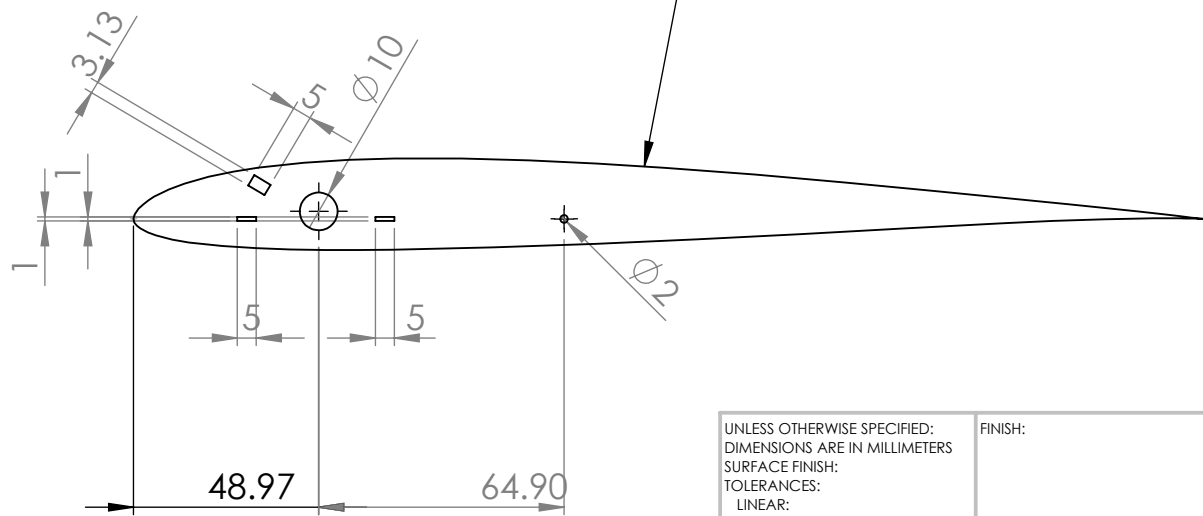
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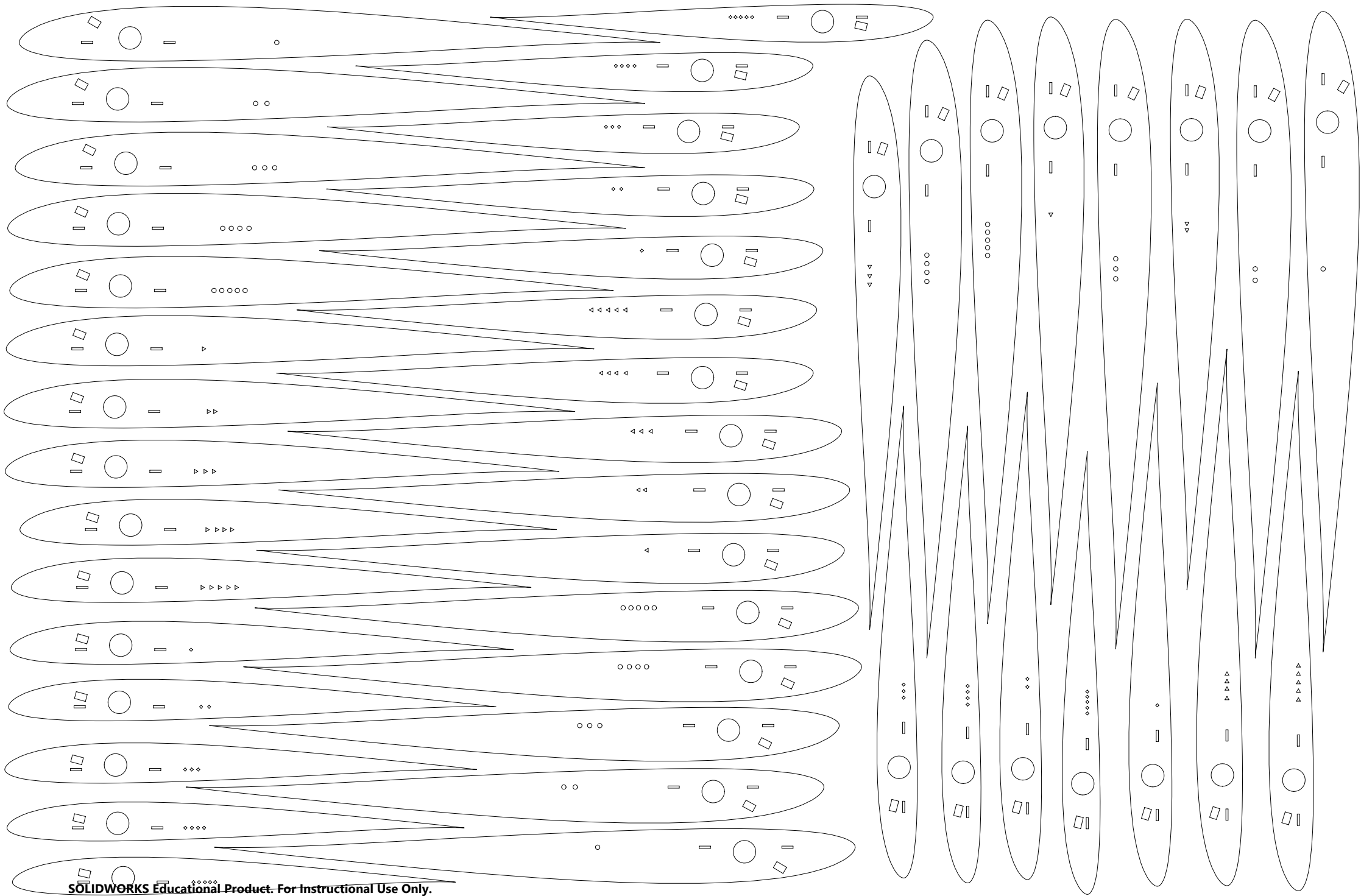


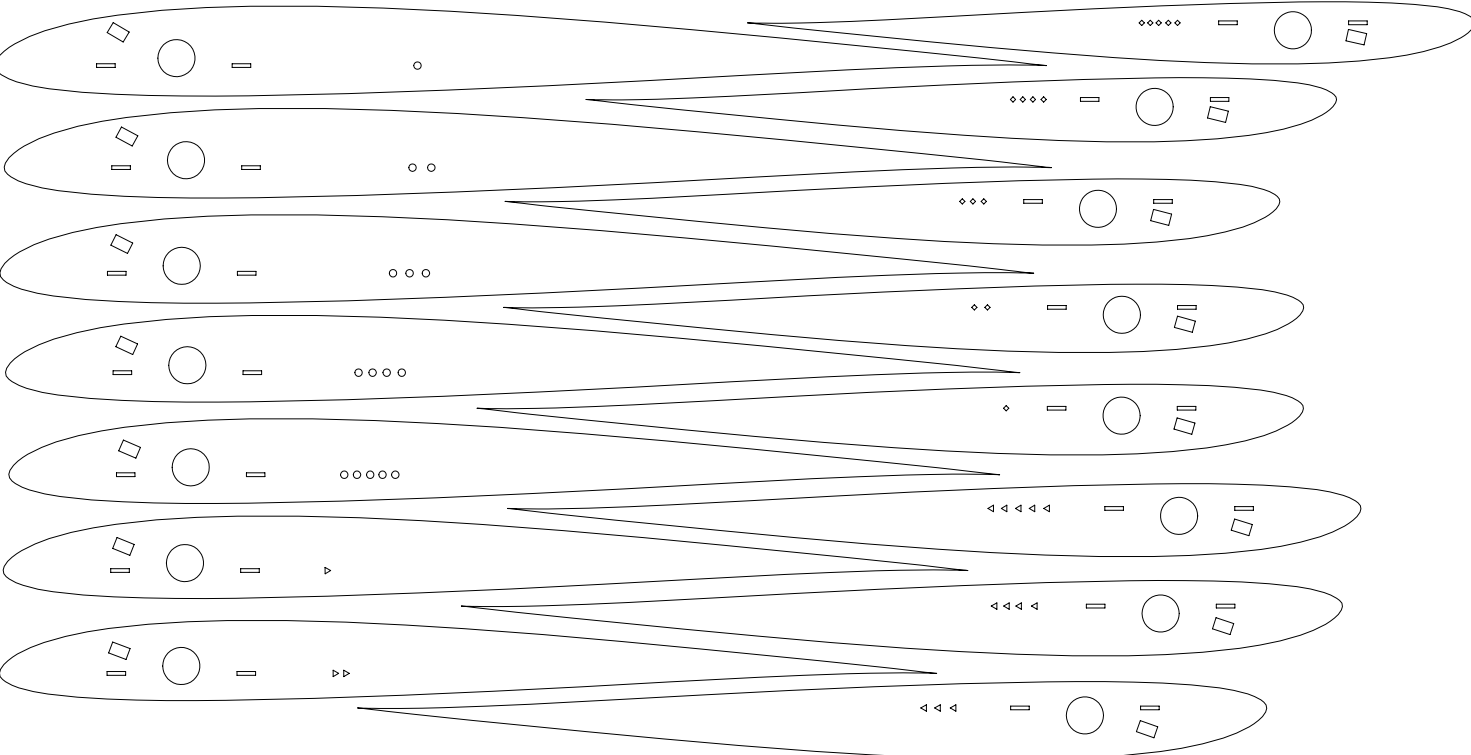
Section One. The remaining sections have then same design, only with changing chordlengths and therefore thickness.



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Eight horizontal rectangular boxes stacked vertically, intended for handwritten notes or answers.

6

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4

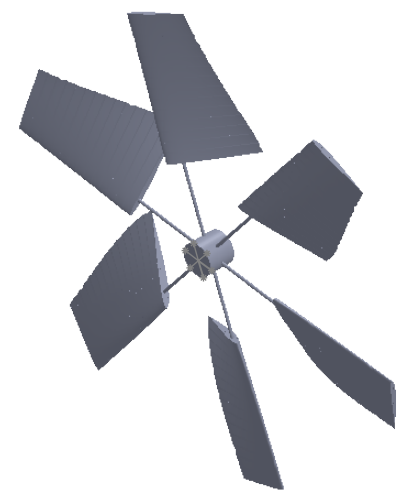
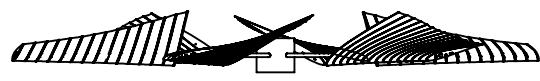
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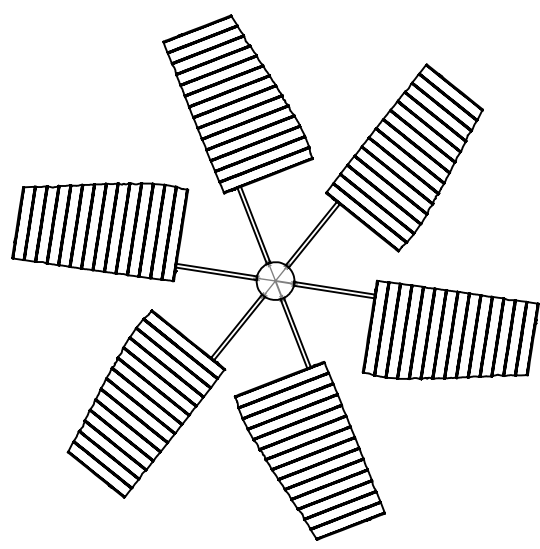
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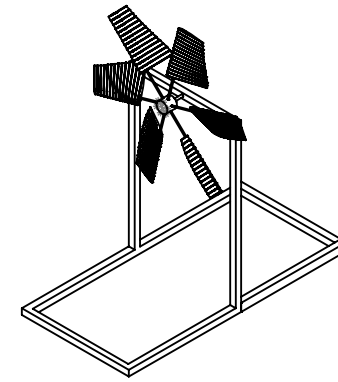
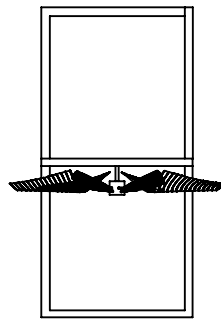
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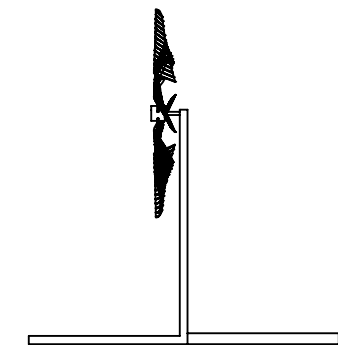
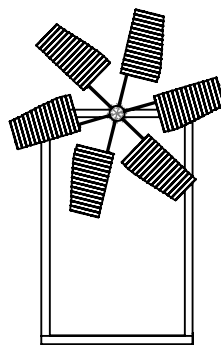
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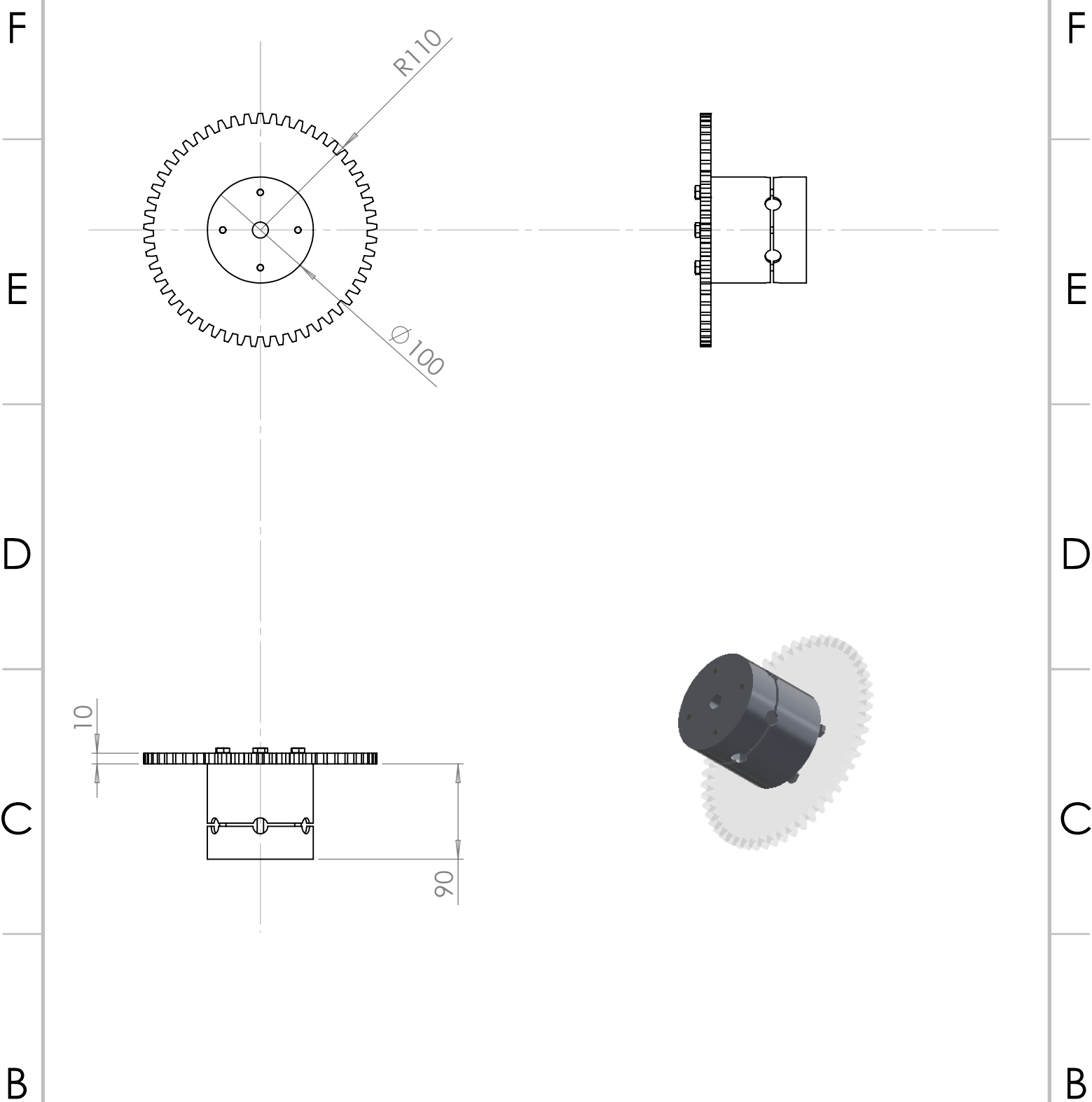
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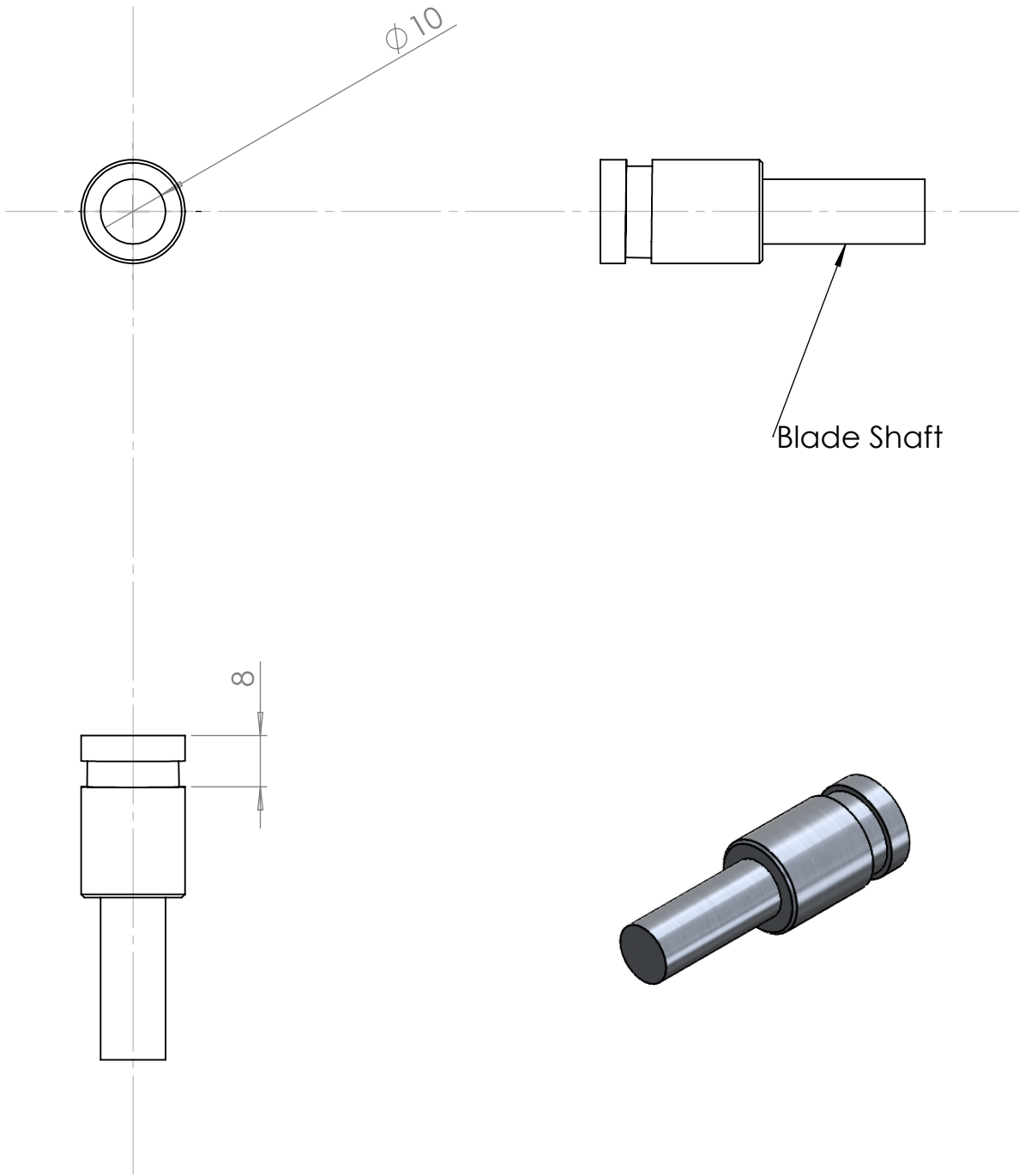
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Appendix A.1: Technical Drawing - Turbine Hub



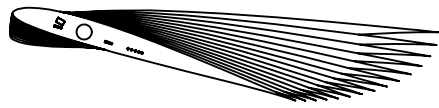
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Appendix A.2: Technical Drawing - Blade Shaft / Connector

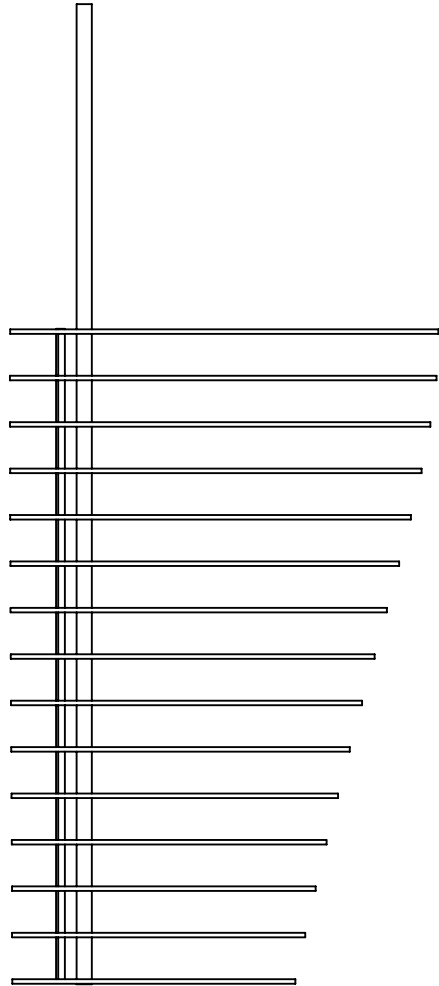
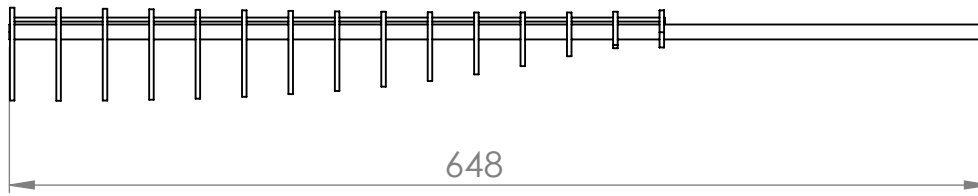


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6 5 4 3 2 1



∅ 10



UNLESS OTHERWISE SPECIFIED: DIMENSIONS ARE IN MILLIMETERS SURFACE FINISH: TOLERANCES: LINEAR: ANGULAR:			FINISH:		DEBURR AND BREAK SHARP EDGES		DO NOT SCALE DRAWING		REVISION		
DRAWN Connor McDowall			SIGNATURE		DATE		TITLE: Blade Assembly				
CHK'D							DWG NO. blade_assem		A4		
APPVD							SCALE:1:10		SHEET 1 OF 1		
MFG							WEIGHT:				
Q.A											

6 5 4 3 2 1

D
C
B
A

D
C
B
A

6

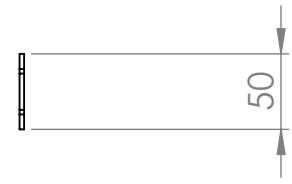
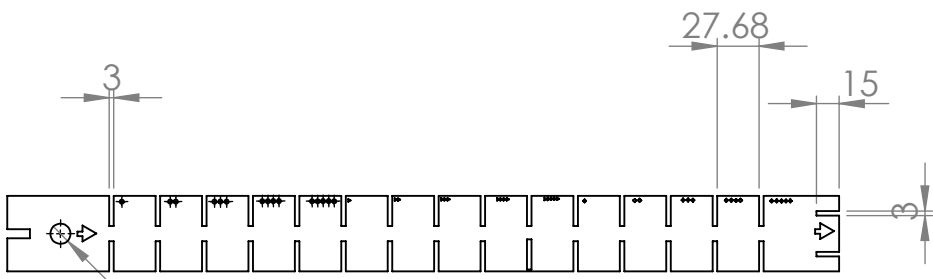
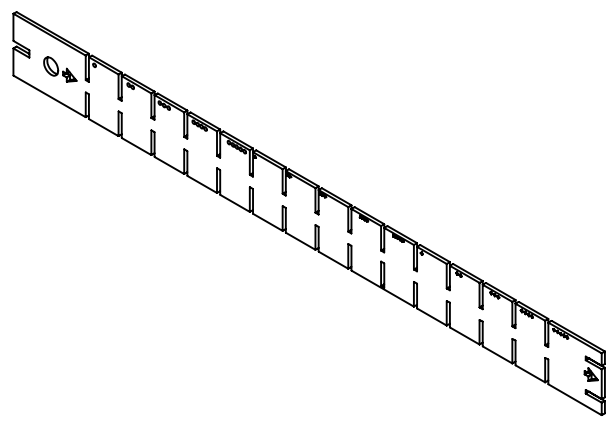
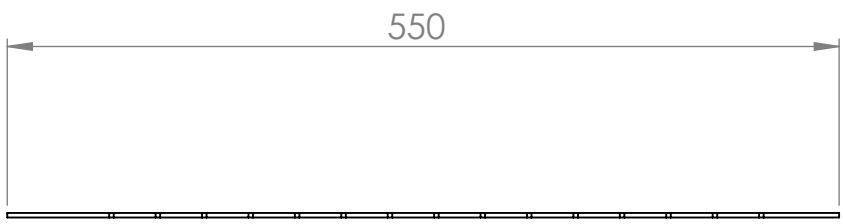
5

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$\varnothing 13.39$

UNLESS OTHERWISE SPECIFIED: DIMENSIONS ARE IN MILLIMETERS SURFACE FINISH: TOLERANCES: LINEAR: ANGULAR:			FINISH:		DEBURR AND BREAK SHARP EDGES		DO NOT SCALE DRAWING		REVISION		
							TITLE: Blade Distance Setting Tool				
DRAWN Connor McDowall			SIGNATURE		DATE				DWG NO. Guide		
CHK'D							MATERIAL:		A4		
APPVD									SCALE:1:5		
MFG									SHEET 1 OF 1		
Q.A							WEIGHT:				

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D

C

C

B

B

A

A

6

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D

C

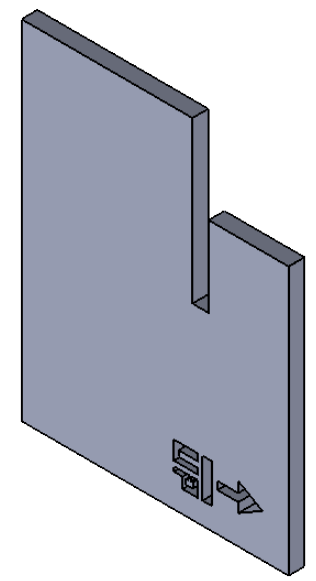
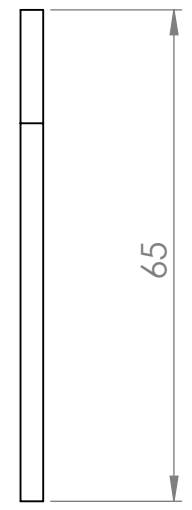
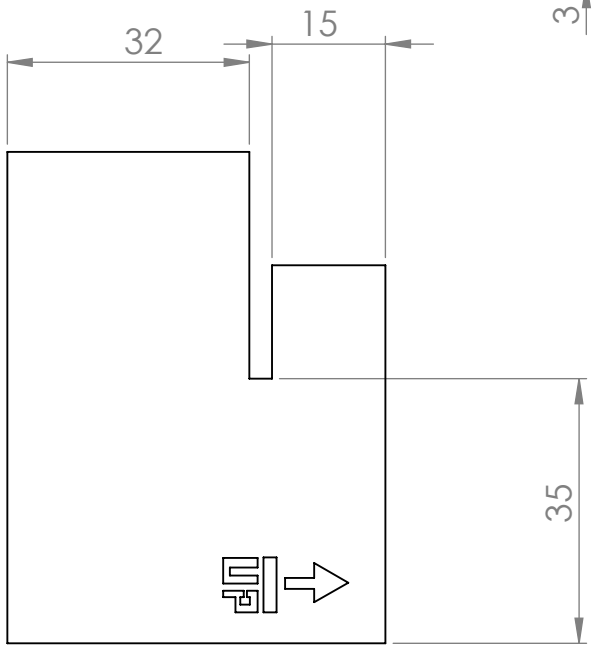
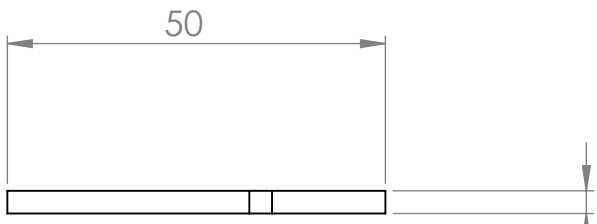
C

B

B

A

A



UNLESS OTHERWISE SPECIFIED: DIMENSIONS ARE IN MILLIMETERS SURFACE FINISH: TOLERANCES: LINEAR: ANGULAR:			FINISH:		DEBURR AND BREAK SHARP EDGES		DO NOT SCALE DRAWING		REVISION	
DRAWN Connor McDowall			SIGNATURE		DATE		TITLE: Stand for the Blade Distance Setting Tool			
CHK'D							DWG NO.		A4	
APPV'D							Stand			
MFG							SCALE:1:1		SHEET 1 OF 1	
Q.A					MATERIAL:					
					WEIGHT:					

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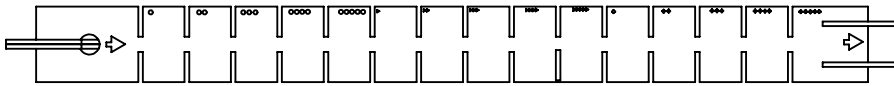
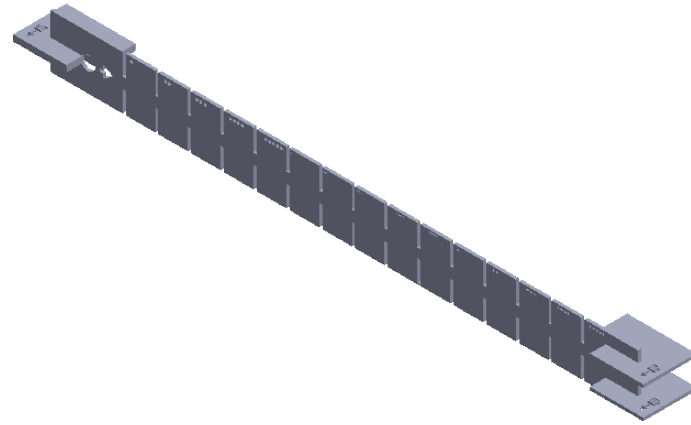
1

D

C

B

A



UNLESS OTHERWISE SPECIFIED: DIMENSIONS ARE IN MILLIMETERS			FINISH:		DEBURR AND BREAK SHARP EDGES		DO NOT SCALE DRAWING		REVISION	
SURFACE FINISH:										
TOLERANCES:										
LINEAR:										
ANGULAR:										
DRAWN		NAME	SIGNATURE	DATE			TITLE:			
		Connor McDowall					Blade Setting Tool Assembly			
CHK'D										
APPV'D										
MFG										
Q.A					MATERIAL:		DWG NO.		A4	
							GuideAssem			
					WEIGHT:		SCALE:1:5		SHEET 1 OF 1	

6

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3

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1

4.5 Analysis: A Nine-Step Process

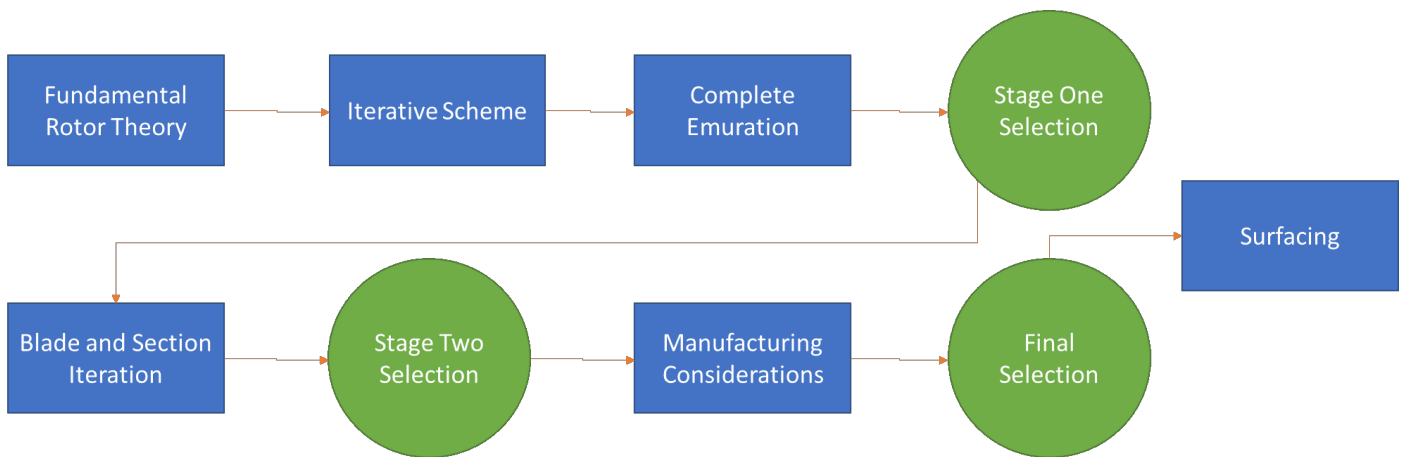


Figure 4: Method of Analysis: A Nine Step Process

5 Fundamental Rotor Theory

See the pdf files on canvas for lectures three to eight covering the fundamental rotor theory. Follow the link below.

”<https://canvas.auckland.ac.nz/courses/30227/files/folder/Lecture%20Slides?>”

5.1 Iterative Scheme

Listing 1: XfoilIteration

```
1 % This Script iterates through all aerofoil designs, trying to find the
2 % best combination for one aerofoil type.
3
4 % Convert Airfoil Bank (Toggle via commenting)
5 bank = dir('airfoil bank');
6 foilnames = {bank.name};
7
8 % Set up the good aerofoils (Toggle via commenting)
9 good = dir('Good');
10 goodfoils = {good.name};
11
12 % Read adjust names to get the data files
13 for i = 1:length(goodfoils)
14     temp = strsplit(goodfoils{i}, '.');
15     goodfoils{i} = strcat(convertCharsToStrings(temp(1)), '.dat');
16 end
17
18 % Chosen design (Toggle via Commenting)
19 goodfoils = {'sd7003.dat', 'sd7003.dat', 'sd7003.dat'};
20
21 % Set the global variables
22 global Vu RPM rho torque eta nSections hubRadius B Re ReRange Storage
23
```

```

24 Vu = 10* 0.51444; % Design speed, e.g. 10 knots an hour (Range: 8/10/12
    knots).
25 RPM = 140; % Target RPM
26 rho = 1.29; % Density of air
27 torque = 3.25; % Target torque, from datasheet
28 eta = 1; % System efficiency
29 nSections = 15;
30 hubRadius = 0.26; % Radius of hub + any further radius with no blade
    allowed
31 B = 6; % Number of blades (Set the appropriate number of
    blades).
32 Re = 60000; % Approximate Reynolds number for design,
33 ReRange = 40000:10000:80000;
34 Storage = 'H:\ENGSCI 363 BEM\BEM\clcdfigures'; %Storage String Directory
35
36 % Saving variables
37 SheetNum = 2;
38 iteration =6;
39 Count = 1;
40 max = 40;
41
42 % Create a for loop for setp through evaluate (changed as the design
43 % process, currently set up to text final design).
44 for i = 3:length(goodfoils)
45     disp(goodfoils{i})
46     % Call evaluate turbine
47     try
48         % Create the figure for the aerofoil
49         [savefile] = evaluatePlot(foilnames{i});
50         % Get parameters fro the aerofoil.
51         [~, design1] = evaluateTurbine(goodfoils{i});
52         % Create a Table
53         name = goodfoils{i};
54         T = table({name},design1.Cp, design1.blades ,design1.nSections,
                    design1.Windspeed,design1.alpha, design1.Re, design1.r,
                    design1.chord, design1.beta);
55         T(1,:);
56         % Save this table to an excel file
57         filename = 'FinalIterations.xlsx';
58         writetable(T,filename, 'Sheet', SheetNum, 'Range',strcat('A',
                    num2str(i+1+iteration*max)), 'WriteVariableNames', false)
59         Count = Count + 1;
60     catch
61     end
62 end

```

Listing 2: evaluateTurbine

```

1 function [obj, design] = evaluateTurbine(varargin)
2 % This function evaluates a turbine design, given a set of properties in
    a
3 % format suitable for optimisation using the metaheuristics code by Yang
    .
4 % 1 Input: x - either a string that contains the ONE aerofoil type to

```

```

be
5 %          used, or else a cell array that contains the aerofoil
type
6 %          at each cross-section.
7 %          -- OR --
8 % 4 Inputs: for aerofoil information already found from elsewhere
9 %          Inputs must be in correct order.
10 %         1. x = 1 x n matrix containing the sequence number (1...k)
of the
11 %             aerofoil to be used at each section. n == nSections
12 %         2. CL = 1 x k matrix containing lift coefficient for each of
k
13 %             aerofoils
14 %         3. CD = 1 x k matrix containing drag coefficient at optimal
angle
15 %             of attack for each of k aerofoils.
16 %         4. alpha = 1 x k matrix containing optimal angle of attack
for
17 %             each of k aerofoils
18 % Outputs: obj = objective value of interest, to be defined for the
application.
19 %         design = structure with turbine design features,
specifically
20 %             r = cross-sectional radii
21 %             chord = chord length
22 %             Cp = power coefficient
23 %             alpha = angle of attack
24 %             beta = local twist angles
25
26 % Connor McDowall cmcd398 530913386
27
28 % Constants (to go into params)
29 global Vu RPM rho torque eta nSections hubRadius B Re
30 mach = 0;
31 % Extract names if one cell input.
32 if nargin == 1
33     x = varargin{1};
34     if isa(x, 'cell')
35         assert(nSections == length(x))
36     else
37         x = cellstr(x);
38     end
39
40 % Find the unique items in the cell array
41 unique_xfoil = unique(x);
42 % Use a loop to step through and the optimum ratios.
43 % Initialise alpha values.
44 alpha_loop = 0:0.5:15;
45 for j = 1:length(unique_xfoil)
46     % Call X foil to get alpha, CD and CL of that cell array.
47     [pol,~] = callXfoil(unique_xfoil{j},alpha_loop , Re, mach);
48     % Find index position of the max ratio
49     [~,i] = max((pol.CL./pol.CD));

```



```

50     % Save the CD, CL and alpha values of the max CL/CD ratio
       position
51     Cdsave = pol.CD(i);
52     Clsave = pol.CL(i);
53     alphasave = deg2rad(alpha_loop(i));
54     % Use a loop to step through the length array and place CD, CL
       and
55     % alpha values of unique_xfoil of the same type.
56     for k = 1:length(x)
57         if x{k} == unique_xfoil{j}
58             Cd(k) = Cdsave;
59             Cl(k) = Clsave;
60             alpha(k) = alphasave;
61         end
62     end
63 end
64
65 elseif nargin == 4
66     % Aerofoil info already pre-generated and is read in.
67     x = varargin{1};
68     assert(nSections == length(x));
69     LiftCoeffs = varargin{2};
70     DragCoeffs = varargin{3};
71     Alphas = varargin{4};
72
73     Cl = LiftCoeffs(x); % Lift coeff for EACH cross-section
74     Cd = DragCoeffs(x); % Drag coeff for EACH cross-section
75     alpha = Alphas(x); % angle of attack for each aerofoil at EACH cross
       -section
76 else
77     error("Incorrect number of inputs")
78 end
79
80 % BEM Calculations
81 % Establish Power requirement and estimate Cp.
82 omega = (RPM.*2.*pi().)/60);
83 Ps = omega.*torque;
84 iterate = true;
85 Cp = 0.593; % Benz Limit
86 % Create the loop to iterate until Cp converges.
87 while iterate == true
88     % Calculate the overall rotor radius
89     R = sqrt((2.*Ps./(Cp.*eta.*rho.*pi().*Vu.^3)));
90
91     % Individual Blade Radius, radia of all aerofoil locations.
92     rind = linspace(hubRadius, R,nSections) ;
93
94     % Calculate the individual wind speed ratios, from the centre of the
95     % blade
96     lambda_ind = (omega.*(rind)./Vu);
97
98     % Calculate the local wind angle and chord length off each section.
99     % This is with wake rotation.

```

```

100 phiw = (2./3)*atan(1./lambda_ind); % radians
101 cwake = ((8.*pi().*(rind))./(B.*Cl)).*(1 - cos(phiw));
102
103 % Calculate the blade setting angles in degrees
104 beta = (180./pi()).*(phiw- alpha) ;
105
106 % Calculate the axial induction factors
107 % Get the constants
108 Cn = Cl.*cos(phiw) + Cd.*sin(phiw);
109 Ct = Cl.*sin(phiw) - Cd.*cos(phiw);
110 f = ((B*(R - rind))./(2.*(rind).*sin(phiw))); % Check r = Rotor
    Radius/ Number of sections
111 F = (2./pi()).*acos(exp(-f));
112
113 % Calculate the blade solidity
114 sigmaprime = (B.*cwake./(2.*pi().*rind));
115
116 % Axial induction factor
117 a = (sigmaprime.*Cn)./(4.*F.*(sin(phiw)).^2 + sigmaprime.*Cn);
118
119 % Calculate the tangential load at each cross section
120 pt = (0.5.*rho.*((Vu.^2).*((1-a).^2)./(sin(phiw).^2))).*Ct.*cwake;
121
122 % Integrate between sections to find the total torque between the
123 % cross sections.
124 Q = B.*trapz(rind,pt.*rind);
125
126 % Find the power extracted and the power available to the wind,
    therefore
127 % finding the power co-efficient Cp
128 Pe = Q.*omega;
129 Pt = 0.5.*rho.*pi().*(R.^2).*(Vu.^3);
130 Cp_iterate = Pe./Pt;
131
132 % Control the looping
133 if abs(Cp_iterate - Cp)<=eps
134     % Reset looping variable if it has converged.
135     iterate = false;
136 end
137 Cp = Cp_iterate;
138 end
139
140 % Store the things in a structure
141 % Define the objective function
142 obj = Cp;
143 % Blade design parameters
144 design = struct('r',rind,'chord',cwake,'Cp',Cp,'alpha',alpha,'beta',beta
    , 'blades',B,'Re',Re,'nSections',nSections,'Windspeed',Vu,'Torque',Q,'
    Power',Pe,'PowerSystem',Pt);
145 %performance = struct('Reynolds Number',Re,'Wind speed',Vu,'Torgue',Q, '
    Power',Pe,'Power Coefficient',Cp);
146 return

```

Listing 3: evaluatePlot

```

1 function [savefile] = evaluatePlot(varargin)
2 % This function evaluates the Cl and Cd, given a set of properties in a
3 % format suitable for optimisation using the metaheuristics code by Yang
4 % 1 Input:  x - either a string that contains the ONE aerofoil type to
5 %           be
6 %           used, or else a cell array that contains the aerofoil
7 %           type
8 %           at each cross-section.
9 %           -- OR --
10 % 4 Inputs: for aerofoil information already found from elsewhere
11 %            Inputs must be in correct order.
12 %            1. x = 1 x n matrix containing the sequence number (1...k)
13 %            of the
14 %            aerofoil to be used at each section. n == nSections
15 %            2. CL = 1 x k matrix containing lift coefficient for each of
16 %            k
17 %            aerofoils
18 %            3. CD = 1 x k matrix containing drag coefficient at optimal
19 %            angle
20 %            of attack for each of k aerofoils.
21 %            4. alpha = 1 x k matrix containing optimal angle of attack
22 %            for
23 %            each of k aerofoils
24 % Outputs:  Location of the saved image for the matlab
25 %            savefile = File Location of saved image
26
27 % Connor McDowall cmcd398 530913386
28 % Clear Figure
29 clf;
30
31 % Constants (to go into params)
32 global nSections ReRange Storage
33 mach = 0;
34 % Extract names if one cell input.
35 if nargin == 1
36     x = varargin{1};
37     if isa(x, 'cell')
38         assert(nSections == length(x))
39     else
40         x = cellstr(x);
41     end
42
43 % Find the unique items in the cell array
44 unique_xfoil = unique(x);
45 % Use a loop to step through and the optimum ratios.
46 % Initialise alpha values and legend
47 plotLegend = {};
48 alpha_loop = 0:1:15;
49 for p = 1:length(ReRange)
50     for j = 1:length(unique_xfoil)
51         % Call X foil to get alpha, CD and CL of that cell array.

```

```

46     [pol, ~] = callXfoil(unique_xfoil{j}, alpha_loop , ReRange(p),
47         mach);
48     % Plot the Cl/CD Function in each iteration of the loop.
49     plot(pol.alpha, (pol.CL./pol.CD))
50     plotLegend{p} = num2str(ReRange(p));
51     hold on
52 end
53
54 %Name and Label plot
55 ylabel('Ratio: Cl/Cd')
56 xlabel('Alpha (Degrees)')
57 split = strsplit(unique_xfoil{1}, '.');
58 foil = strcat(split{1}, '.png');
59 title(split) % Assuming only one aerofoil is passed in.
60 legend(plotLegend);
61 % Show the figure
62 figure(gcf);
63 % Save the figure to the current directory.
64 savefile = fullfile(Storage, foil);
65 saveas(gcf, savefile);
66
67 else
68     error("Incorrect number of inputs")
69 end

```

Listing 4: callXfoil

```

1 function [pol, foil] = callXfoil(coord, alpha, Re, Mach)
2 % This function acts as a general interface to xfoil.m by Louis Edelmann
3 % :
4 % https://au.mathworks.com/matlabcentral/fileexchange/49706-xfoil-
5 % interface-updated
6 %
7 % Inputs: coord = coordinates of aerofoil.
8 %           3 cases: 1. 'NACAxxxxx' for NACA 4 or 5 digits
9 %                   2. 'xxxx.dat' for an aerofoil in the
10 %                   airfoil
11 %                   bank.
12 %                   3. an n by 2 array of x and y
13 %                   coordinates.
14 %           For non NACA cases, 300 panel points are
15 %           interpolated to
16 %           hopefully give convergence. In all cases, max 100
17 %           iterations are run.
18 %           alpha = angle(s) of attack to consider Re = Reynold's number
19 %           of
20 %           interest. Mach = Mach number of interest. Typically 0 for
21 %           non-turbulent flow.
22 % Outputs: see xfoil.m
23 %
24 % This code is supplied with an adapted version of the UIUC Airfoil
25 % Database (http://m-selig.ae.illinois.edu/ads/coord\_database.html) by
26 % Michael Selig. Divahar Jayaraman adapted these to a consistent format

```

```

    in
22 % her code for 2D Potential Flows, as found below...
23 % http://au.mathworks.com/matlabcentral/fileexchange/12790-panel-method-
    based-2-d-potential-flow-simulator
24 % This is used by loading the 'airfoil bank' folder into the path when
25 % needed.
26 %
27 % Kevin Jia, UoA EngSci, 2017.
28
29 if isa(coord, 'char') == true && strcmp(coord(1:4), 'NACA') == true
30     % A built in NACA airfoil.
31     [pol,foil] = xfoil(coord, alpha, Re, Mach, 'PLOP G', 'pane ppar n
        300/', 'oper/iter 200');
32 elseif isa(coord, 'char') == true && strcmp(coord(length(coord)-3:length
    (coord)), '.dat')
33     % An aerofoil in the airfoil bank folder.
34     addpath('airfoil bank')
35     if exist(coord)
36         % Import data, first remove heading.
37         data = importdata(coord, ' ', 1);
38         coordinates = data.data;
39         [pol,foil] = xfoil(coordinates, alpha, Re, Mach, 'PLOP G', 'pane
        n 300/', 'oper/iter 200');
40     else
41         error('.dat file does not exist')
42     end
43
44 else
45     % 2D array of coordinates
46     [pol,foil] = xfoil(coord, alpha, Re, Mach, 'PLOP G', 'pane n 200/', '
        oper/iter 100');
47 end
48
49 pol = checkPol(pol, alpha);
50
51 return
52
53 function polOut = checkPol(polIn, alpha)
54
55 if length(polIn.alpha) ~= length(alpha)
56     % Lengths do not match, need to do an interpolation for some angle(s
        ).
57
58     % Copy structure
59     polOut = polIn;
60     % Find missing angles
61     existingInds = ismember(alpha', polIn.alpha);
62     missingInds = ~ismember(alpha', polIn.alpha);
63     needToFind = alpha(missingInds);
64     missingLifts = interp1(polIn.alpha, polIn.CL, needToFind);
65     missingDrags = interp1(polIn.alpha, polIn.CD, needToFind);
66
67     allLifts(existingInds) = polIn.CL;

```

```

68     allLifts(missingInds) = missingLifts;
69
70     allDrags(existingInds) = polIn.CD;
71     allDrags(missingInds) = missingDrags;
72
73     polOut.CL = allLifts';
74     polOut.CD = allDrags';
75     polOut.alpha = alpha';
76
77 else
78     polOut = polIn;
79 end
80
81 return

```

Listing 5: xfoil.m

```

1 function [pol,foil] = xfoil(coord,alpha,Re,Mach,varargin)
2 % Run XFOil and return the results.
3 % [polar,foil] = xfoil(coord,alpha,Re,Mach,{extra commands})
4 %
5 % Xfoil.exe needs to be in the same directory as this m function.
6 % For more information on XFOil visit these websites;
7 % http://web.mit.edu/drela/Public/web/xfoil
8 %
9 % Inputs:
10 %   coord: Normalised foil co-ordinates (n by 2 array, of x & y
11 %         from the TE-top passed the LE to the TE bottom)
12 %         or a filename of the XFOil co-ordinate file
13 %         or a NACA 4 or 5 digit descriptor (e.g. 'NACA0012')
14 %   alpha: Angle-of-attack, can be a vector for an alpha polar
15 %   Re: Reynolds number (use Re=0 for inviscid mode)
16 %   Mach: Mach number
17 % extra commands: Extra XFOil commands
18 %                 The extra XFOil commands need to be proper xfoil commands
19 %                 in a character array. e.g. 'oper/iter 150'
20 %
21 % The transition criterion Ncrit can be specified using the
22 % 'extra commands' option as follows,
23 % foil = xfoil('NACA0012',10,1e6,0.2,'oper/vpar n 12')
24 %
25 %   Situation           Ncrit
26 %   -----
27 %   sailplane           12-14
28 %   motorglider         11-13
29 %   clean wind tunnel   10-12
30 %   average wind tunnel 9 <= standard "e^9 method"
31 %   dirty wind tunnel   4-8
32 %
33 % A flap deflection can be added using the following command,
34 % 'gdes flap {xhinge} {yhinge} {flap_defelction} exec'
35 %
36 % Outputs:
37 %   polar: structure with the polar coefficients (alpha,CL,CD,CDp,CM,

```

```

38 %         Top_Xtr,Bot_Xtr)
39 %   foil: structure with the specific aoa values (s,x,y,UeVinf,
40 %         Dstar,Theta,Cf,H,cpx,cp) each column corresponds to a
         different
41 %         angle-of-attack.
42 %         If only one left hand operator is specified, only the polar
         will be parsed and output
43 %
44 % If there are different sized output arrays for the different incidence
45 % angles then they will be stored in a structured array, foil(1),foil(2)
         ...
46 %
47 % If the output array does not have all alphas in it, that indicates a
         convergence failure in Xfoil.
48 % In that event, increase the iteration count with 'oper iter ##';
49 %
50 % Examples:
51 %   % Single AoA with a different number of panels
52 %   [pol foil] = xfoil('NACA0012',10,1e6,0.0,'panels n 330')
53 %
54 %   % Change the maximum number of iterations
55 %   [pol foil] = xfoil('NACA0012',5,1e6,0.2,'oper iter 50')
56 %
57 %   % Deflect the trailing edge by 20deg at 60% chord and run multiple
         incidence angles
58 %   [pol foil] = xfoil('NACA0012',[-5:15],1e6,0.2,'oper iter 150','gdes
         flap 0.6 0 5 exec')
59 %   % Deflect the trailing edge by 20deg at 60% chord and run multiple
         incidence angles and only
60 %   parse or output a polar.
61 %   pol = xfoil('NACA0012',[-5:15],1e6,0.2,'oper iter 150','gdes flap
         0.6 0 5 exec')
62 %   % Plot the results
63 %   figure;
64 %   plot(pol.alpha,pol.CL); xlabel('alpha [\circ]'); ylabel('C_L');
         title(pol.name);
65 %   figure; subplot(3,1,[1 2]);
66 %   plot(foil(1).xcp(:,end),foil(1).cp(:,end)); xlabel('x');
67 %   ylabel('C_p'); title(sprintf('%s @ %g\circ',pol.name,foil(1).alpha
         (end)));
68 %   set(gca,'ydir','reverse');
69 %   subplot(3,1,3);
70 %   I = (foil(1).x(:,end)<=1);
71 %   plot(foil(1).x(I,end),foil(1).y(I,end)); xlabel('x');
72 %   ylabel('y'); axis('equal');
73 %
74
75 % Some default values
76 if ~exist('coord','var'), coord = 'NACA0012'; end;
77 if ~exist('alpha','var'), alpha = 0;     end;
78 if ~exist('Re','var'),   Re = 1e6;      end;
79 if ~exist('Mach','var'), Mach = 0.2;    end;
80 Nalpha = length(alpha); % Number of alphas swept

```

```

81 % default foil name
82 foil_name = mfilename;
83
84 % default filenames
85 wd = fileparts(which(mfilename)); % working directory, where xfoil.exe
    needs to be
86 fname = mfilename;
87 file_coord= [foil_name '.foil'];
88
89 % Save coordinates
90 if ischar(coord), % Either a NACA string or a filename
91     if isempty(regexpi(coord, '^NACA *[0-9]{4,5}$')) % Check if a NACA
        string
92 %     foil_name = coord; % some redundant code removed to go green ( ~
        isempty if uncommented)
93 %     else % Filename supplied
94 %     set coord file
95     file_coord = coord;
96 end;
97 else
98 % Write foil ordinate file
99 if exist(file_coord, 'file'), delete(file_coord); end;
100 fid = fopen(file_coord, 'w');
101 if (fid<=0),
102     error([mfilename ':io'], 'Unable to create file %s', file_coord);
103 else
104     fprintf(fid, '%s\n', foil_name);
105     fprintf(fid, '%9.5f %9.5f\n', coord);
106     fclose(fid);
107 end;
108 end;
109
110 % Write xfoil command file
111 fid = fopen([wd filesep fname '.inp'], 'w');
112 if (fid<=0),
113     error([mfilename ':io'], 'Unable to create xfoil.inp file');
114 else
115     if ischar(coord),
116         if ~isempty(regexpi(coord, '^NACA *[0-9]{4,5}$')), % NACA string
            supplied
117             fprintf(fid, 'naca %s\n', coord(5:end));
118         else % filename supplied
119             fprintf(fid, 'load %s\n', file_coord);
120         end;
121     else % Coordinates supplied, use the default filename
122         fprintf(fid, 'load %s\n', file_coord);
123     end;
124 % Extra Xfoil commands
125 for ii = 1:length(varargin),
126     txt = varargin{ii};
127     txt = regexprep(txt, '[ \\\/]+', '\n');
128     fprintf(fid, '%s\n\n', txt);
129 end;

```



```

130 fprintf(fid, '\n\noper\n');
131 % set Reynolds and Mach
132 fprintf(fid, 're %g\n', Re);
133 fprintf(fid, 'mach %g\n', Mach);
134
135 % Switch to viscous mode
136 if (Re>0)
137     fprintf(fid, 'visc\n');
138 end;
139
140 % Polar accumulation
141 fprintf(fid, 'pacc\n\n\n');
142 % Xfoil alpha calculations
143 [file_dump, file_cpwr] = deal(cell(1, Nalpha)); % Preallocate cell
    arrays
144
145 for ii = 1:Nalpha
146     % Individual output filenames
147     file_dump{ii} = sprintf('%s_a%06.3f_dump.dat', fname, alpha(ii));
148     file_cpwr{ii} = sprintf('%s_a%06.3f_cpwr.dat', fname, alpha(ii));
149     % Commands
150     fprintf(fid, 'alfa %g\n', alpha(ii));
151     fprintf(fid, 'dump %s\n', file_dump{ii});
152     fprintf(fid, 'cpwr %s\n', file_cpwr{ii});
153 end;
154 % Polar output filename
155 file_pwrt = sprintf('%s_pwrt.dat', fname);
156 fprintf(fid, 'pwrt\n%s\n', file_pwrt);
157 fprintf(fid, 'plis\n');
158 fprintf(fid, '\nquit\n');
159 fclose(fid);
160
161 % execute xfoil
162 cmd = sprintf('cd %s && xfoil.exe < xfoil.inp > xfoil.out', wd);
163 [status, result] = system(cmd);
164 if (status~=0),
165     disp(result);
166     error([mfilename ':system'], 'Xfoil execution failed! %s', cmd);
167 end;
168
169 % Read dump file
170 %   #       s           x           y       Ue/Vinf       Dstar       Theta       Cf
        H
171 jj = 0;
172 ind = 1;
173 % Note that
174 foil.alpha = zeros(1, Nalpha); % Preallocate alphas
175 % Find the number of panels with an initial run
176 only = nargout; % Number of outputs checked. If only one left hand
    operator then only do polar
177
178 if only >1 % Only do the foil calculations if more than one left hand
    operator is specified

```

```

179 for ii = 1:Nalpha
180     jj = jj + 1;
181
182     fid = fopen([wd filesep file_dump{ii}], 'r');
183     if (fid<=0),
184         error([mfilename ':io'], 'Unable to read xfoil output file %s',
185             file_dump{ii});
186     else
187         D = textscan(fid, '%f%f%f%f%f%f%f', 'Delimiter', ' ', '
188             MultipleDelimsAsOne', true, 'CollectOutput', 1, 'HeaderLines', 1);
189         fclose(fid);
190         delete([wd filesep file_dump{ii}]);
191
192         if ii == 1 % Use first run to determine number of panels (so that
193             NACA airfoils work without vector input)
194             Npanel = length(D{1}); % Number of airfoil panels pulled from
195                 the first angle tested
196             % Preallocate Outputs
197             [foil.s, foil.x, foil.y, foil.UeVinf, foil.Dstar, foil.Theta,
198                 foil.Cf, foil.H] = deal(zeros(Npanel, Nalpha));
199         end
200
201         % store data
202         if ((jj>1) && (size(D{1}, 1)~=length(foil(ind).x)) && sum(abs(foil(
203             ind).x(:, 1)-size(D{1}, 1)))>1e-6 ),
204             ind = ind + 1;
205             jj = 1;
206         end;
207         foil.s(:, jj) = D{1}(:, 1);
208         foil.x(:, jj) = D{1}(:, 2);
209         foil.y(:, jj) = D{1}(:, 3);
210         foil.UeVinf(:, jj) = D{1}(:, 4);
211         foil.Dstar(:, jj) = D{1}(:, 5);
212         foil.Theta(:, jj) = D{1}(:, 6);
213         foil.Cf(:, jj) = D{1}(:, 7);
214         foil.H(:, jj) = D{1}(:, 8);
215     end;
216
217     foil.alpha(1, jj) = alpha(jj);
218
219     % Read cp file
220     fid = fopen([wd filesep file_cpwr{ii}], 'r');
221     if (fid<=0),
222         error([mfilename ':io'], 'Unable to read xfoil output file %s',
223             file_cpwr{ii});
224     else
225         C = textscan(fid, '%10f%9f%f', 'Delimiter', ',', 'WhiteSpace', ' ',
226             'HeaderLines', 3, 'ReturnOnError', false);
227         fclose(fid);
228         delete([wd filesep file_cpwr{ii}]);
229         % store data
230         if ii == 1 % Use first run to determine number of panels (so that
231             NACA airfoils work without vector input)

```

```

223         NCp = length(C{1}); % Number of points Cp is listed for pulled
           from the first angle tested
224         % Preallocate Outputs
225         [foil.xcp, foil.cp] = deal(zeros(NCp,Nalpha));
226         foil.xcp = C{1}(:,1);
227     end
228     foil.cp(:,jj) = C{3}(:,1);
229 end;
230 end;
231 end
232
233 if only <= 1% clear files for default run
234     for ii=1:Nalpha % Clear out the xfoil dump files not used
235         delete([wd filesep file_dump{ii}]);
236         delete([wd filesep file_cpwr{ii}]);
237     end
238 end
239
240 % Read polar file
241 %
242 %         XFOIL             Version 6.96
243 %
244 % Calculated polar for: NACA 0012
245 %
246 % 1 1 Reynolds number fixed           Mach number fixed
247 %
248 % xtrf =   1.000 (top)           1.000 (bottom)
249 % Mach =   0.000      Re =       1.000 e 6      Ncrit =  12.000
250 %
251 %   alpha      CL          CD          CDp          CM          Top_Xtr  Bot_Xtr
252 %  -----  -----  -----  -----  -----  -----  -----
253 fid = fopen([wd filesep file_pwrt],'r');
254 if (fid<=0),
255     error([mfilename ':io'],'Unable to read xfoil polar file %s',
           file_pwrt);
256 else
257     % Header
258     % Calculated polar for: NACA 0012
259     P = textscan(fid,' Calculated polar for: %[\n]','Delimiter',' ','
           MultipleDelimsAsOne',true,'HeaderLines',3);
260     pol.name = strtrim(P{1}{1});
261     % xtrf =   1.000 (top)           1.000 (bottom)
262     P = textscan(fid, '%s%s%f%s%f%s%s%s%s', 1, 'Delimiter', ' ',
           'MultipleDelimsAsOne', true, 'HeaderLines', 2, 'ReturnOnError',
           false);
263     pol.xtrf_top = P{1}(1);
264     pol.xtrf_bot = P{2}(1);
265     % Mach =   0.000      Re =       1.000 e 6      Ncrit =  12.000
266     P = textscan(fid, '%s%s%f%s%s%f%s%f%s%s%f', 1, 'Delimiter', '
           ', 'MultipleDelimsAsOne', true, 'HeaderLines', 0, 'ReturnOnError'
           , false);
267     pol.Re = P{2}(1) * 10^P{3}(1);
268     pol.Ncrit = P{4}(1);

```

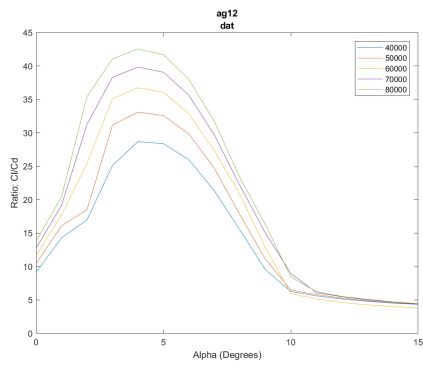
```

269
270 % data
271 P = textscan(fid, '%f%f%f%f%f%f*s*s*s*s', 'Delimiter', ' ', '
    MultipleDelimsAsOne', true, 'HeaderLines' , 4, 'ReturnOnError',
    false);
272 fclose(fid);
273 delete([wd filesep file_pwrt]);
274 % store data
275 pol.alpha = P{1}(:,1);
276 pol.CL = P{2}(:,1);
277 pol.CD = P{3}(:,1);
278 pol.CDp = P{4}(:,1);
279 pol.Cm = P{5}(:,1);
280 pol.Top_xtr = P{6}(:,1);
281 pol.Bot_Xtr = P{7}(:,1);
282 end
283 if length(pol.alpha) ~= Nalpha % Check if xfoil failed to converge
284     warning('One or more alpha values failed to converge. Last
    converged was alpha = %f. Rerun with 'oper iter #' command.\n'
    , pol.alpha(end))
285 end
286
287 end

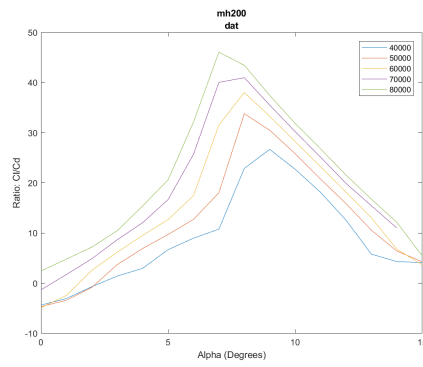
```

5.2 Complete Enumeration

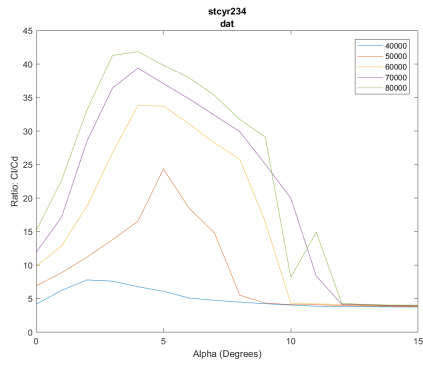
Over 1000 plots were generated. Below is a very small subset to illustrate the concept.



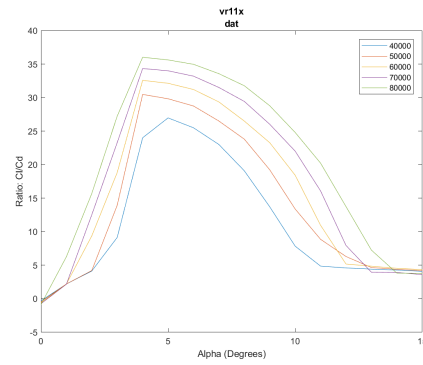
(a) ag12



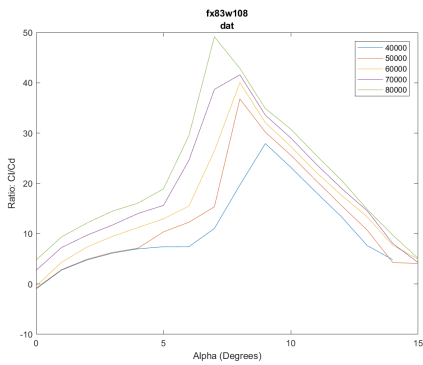
(b) mh200



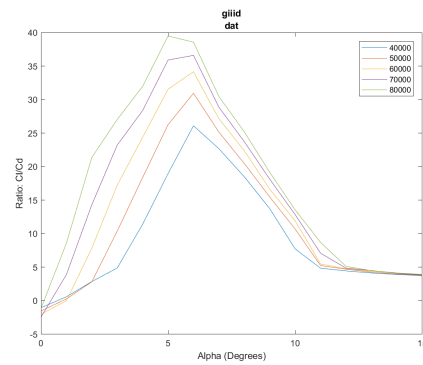
(c) steyr234



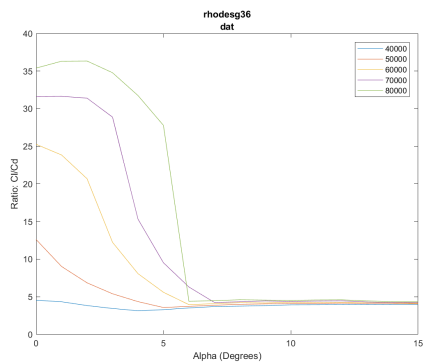
(d) vr11x



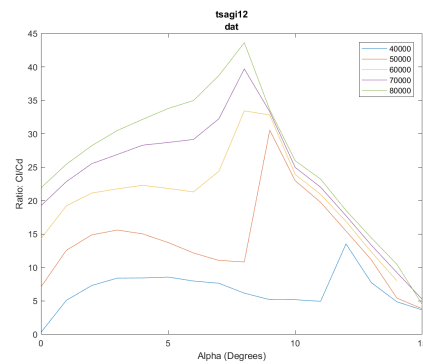
(e) fx83w108



(f) giid



(g) rhodesg36



(h) tsagi12

Figure 5: A Small Subset of the Plots generated during Complete Enumeration

5.3 Stage One Selection

Stage One Selection	
ag03.dat	giiic.dat
ag11.dat	hh02.dat
ag16.dat	ht22.dat
ag455ct02r.dat	isa962.dat
ag45ct02r.dat	lg10sc.dat
ag46c03.dat	mh32.dat
ah7476.dat	mh44.dat
ames01.dat	naca1410.dat
arad10.dat	naca23012.dat
be50.dat	naca23015.dat
boe103.dat	ncambre.dat
deford3.dat	np19615.dat
df101.dat	np19660.dat
e212.dat	rae100.dat
e216.dat	s8025.dat
e222.dat	s9000.dat
fg1.dat	sd7003.dat
fx69h098.dat	v13009.dat
fx76120.dat	

Figure 6: 37 Selected Aerofoils

5.4 Blade and Section Iteration

Name	Cp	# of Blades	# of Sections	Cp	# of Blades	# of Sections	Cp	# of Blades	# of Sections
ag16.dat	0.382113123	4	15	0.398471	6	15	0.415932714	6	15
ag11.dat	0.381574269	4	15	0.398616	6	15	0.416108346	6	15
ag03.dat	0.381436383	4	15	0.39918	6	15	0.416794554	6	15
ag45ct02r.d	0.37999074	4	15	0.396907	6	15	0.414030026	6	15
ag455ct02r	0.379943415	4	15	0.396965	6	15	0.414100994	6	15
sd7003.dat	0.379062469	4	15	0.397078	6	15	0.414238553	6	15
s9000.dat	0.383338597	4	15	0.406572	6	15	0.425757362	6	15
arad10.dat	0.383072989	4	15	0.391169	6	15	0.407033612	6	15
mh44.dat	0.379380573	4	15	0.400186	6	15	0.418016305	6	15
np19615.da	0.378773944	4	15	0.402837	6	15	0.421233543	6	15
np19660.da	0.378076386	4	15	0.399868	6	15	0.417630082	6	15
be50.dat	0.385603462	4	15	0.394314	6	15	0.410871864	6	15
isa962.dat	0.384534587	4	15	0.398732	6	15	0.416249713	6	15
mh32.dat	0.383587864	4	15	0.402648	6	15	0.421004085	6	15
ag46c03.da	0.380106966	4	15	0.404296	6	15	0.423000952	6	15
defcnd3.da	0.377468631	4	15	0.401544	6	15	0.419664783	6	15
fx69h098.d	0.3774145	4	15	0.402117	6	15	0.420360276	6	15
ncambre.d	0.376452056	4	15	0.394257	6	15	0.410802726	6	15
v13009.dat	0.375373694	4	15	0.390909	6	15	0.406716021	6	15
lg10sc.dat	0.37464165	4	15	0.396483	6	15	0.413513605	6	15
ames01.da	0.374466594	4	15	0.397494	6	15	0.414743697	6	15
fx76120.dat	0.374218478	4	15	0.390368	6	15	0.406054985	6	15
ht22.dat	0.373702189	4	15	0.401717	6	15	0.419875215	6	15
s8025.dat	0.371289808	4	15	0.391352	6	15	0.407257652	6	15
ah7476.dat	0.389168471	4	15	0.400725	6	15	0.41867134	6	15
e216.dat	0.38699533	4	15	0.396317	6	15	0.413312228	6	15
e212.dat	0.38542285	4	15	0.397365	6	15	0.414586757	6	15
fg1.dat	0.384916201	4	15	0.390573	6	15	0.406305696	6	15
e222.dat	0.384369063	4	15	0.38958	6	15	0.405091495	6	15
boe103.dat	0.382769489	4	15	0.393249	6	15	0.409573023	6	15
df101.dat	0.381685264	4	15	0.395682	6	15	0.412538283	6	15
hh02.dat	0.380503232	4	15	0.394951	6	15	0.411647935	6	15
naca1410.d	0.380380107	4	15	0.390386	6	15	0.40607767	6	15
g1iic.dat	0.379538456	4	15	0.38784	6	15	0.402963004	6	15
naca23012	0.373897979	4	15	0.400464	6	15	0.418354244	6	15
rae100.dat	0.373719903	4	15	0.395984	6	15	0.412906426	6	15
naca23015	0.372950016	4	15	0.392119	6	15	0.408194236	6	15

(a) One set of changing the Number of Blades with a Fixed Number of Sections

Name	Cp	# of Blades	# of Sections	Cp	# of Blades	# of Sections	Cp	# of Blades	# of Sections
ag03.dat	0.402759219	6	14	0.403931	6	15	0.40490877	6	16
ag11.dat	0.402905735	6	14	0.404078	6	15	0.405055981	6	16
ag16.dat	0.403478333	6	14	0.404652	6	15	0.405631294	6	16
ag455ct02r	0.401172931	6	14	0.40234	6	15	0.403314963	6	16
ag45ct02r.d	0.401232065	6	14	0.4024	6	15	0.403374377	6	16
ag46c03.da	0.401346694	6	14	0.402515	6	15	0.403489549	6	16
ah7476.dat	0.410978179	6	14	0.412171	6	15	0.4131667	6	16
ames01.da	0.395355723	6	14	0.396508	6	15	0.39747018	6	16
arad10.dat	0.404498381	6	14	0.405675	6	15	0.406656177	6	16
be50.dat	0.407187951	6	14	0.408371	6	15	0.409358499	6	16
boe103.dat	0.404175842	6	14	0.405351	6	15	0.40633211	6	16
defcnd3.da	0.398543958	6	14	0.399705	6	15	0.400673527	6	16
df101.dat	0.403023678	6	14	0.404196	6	15	0.405174483	6	16
e212.dat	0.406995962	6	14	0.408179	6	15	0.4091656	6	16
e216.dat	0.4086676	6	14	0.409855	6	15	0.410845164	6	16
e222.dat	0.405875862	6	14	0.407056	6	15	0.408040189	6	16
fg1.dat	0.406457416	6	14	0.407639	6	15	0.408624501	6	16
fx69h098.d	0.398486461	6	14	0.399647	6	15	0.400615758	6	16
fx76120.dat	0.39509226	6	14	0.396244	6	15	0.397205468	6	16
g1iic.dat	0.400742698	6	14	0.401909	6	15	0.402882691	6	16
hh02.dat	0.401767713	6	14	0.402937	6	15	0.403912565	6	16
ht22.dat	0.394544056	6	14	0.395694	6	15	0.396654665	6	16
isa962.dat	0.406051795	6	14	0.407232	6	15	0.408216957	6	16
lg10sc.dat	0.395541611	6	14	0.396695	6	15	0.397656949	6	16
mh32.dat	0.405045575	6	14	0.406223	6	15	0.407205966	6	16
mh44.dat	0.400574967	6	14	0.401741	6	15	0.402714164	6	16
naca1410.d	0.401636896	6	14	0.402806	6	15	0.403781127	6	16
naca23012	0.394751946	6	14	0.395903	6	15	0.396863541	6	16
naca23015	0.393745436	6	14	0.394894	6	15	0.39585226	6	16
ncambre.d	0.397464226	6	14	0.398622	6	15	0.399588678	6	16
np19615.da	0.399930519	6	14	0.401095	6	15	0.402066662	6	16
np19660.da	0.39918952	6	14	0.400352	6	15	0.40132215	6	16
rae100.dat	0.394562865	6	14	0.395713	6	15	0.396673563	6	16
s8025.dat	0.39198292	6	14	0.393127	6	15	0.394081388	6	16
s9000.dat	0.404780657	6	14	0.405958	6	15	0.406939792	6	16
sd7003.dat	0.400237026	6	14	0.401402	6	15	0.402374622	6	16
v13009.dat	0.396318987	6	14	0.397474	6	15	0.39843801	6	16

(b) One set of changing the Number of Sections with a Fixed Number of Blades

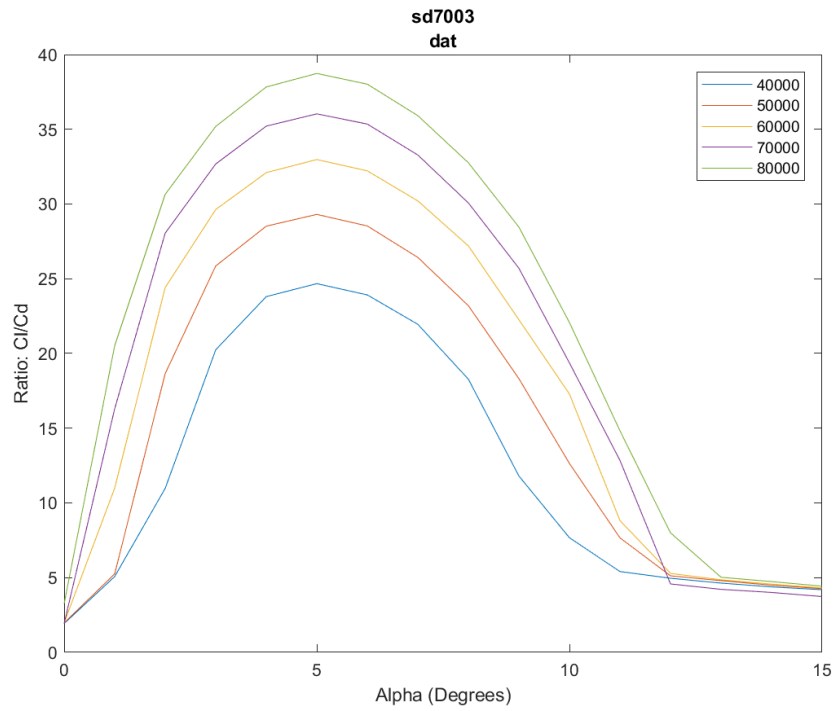
Figure 7: One third of all iterations

5.5 Manufacturing Considerations

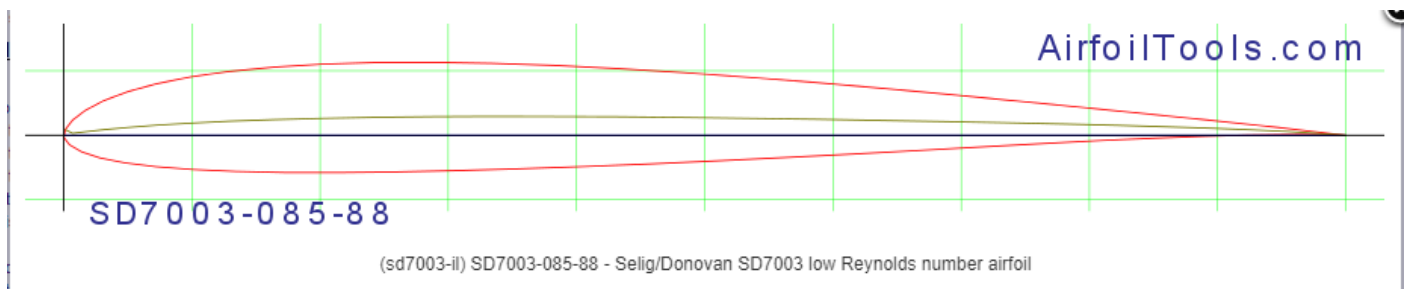
Name	Cp	Number of Blades	Number of Sections	Plot	Thickness	Cambre	Thickness2
ah7476.dat	0.406572	6	15	0	5.9		5.928195341
e216.dat	0.404296	6	15	0	10.4		10.54111723
be50.dat	0.402837	6	15	1	7.3		10.91979226
e212.dat	0.402648	6	15	0	10.6		14.35801718
fg1.dat	0.402117	6	15	0	8.2		13.45957095
isa962.dat	0.401717	6	15	1	9.6		12.29594233
e222.dat	0.401544	6	15	0	10.2		14.83437748
mh32.dat	0.400725	6	15	1	8.7		13.99001317
s9000.dat	0.400464	6	15	2	9		14.84379605
arad10.dat	0.400186	6	15	2	10		15.76392454
boe103.dat	0.399868	6	15	0	12.7		16.32408669
ag16.dat	0.39918	6	15	3	7.1		14.25860086
df101.dat	0.398732	6	15	0	11		17.23135917
ag11.dat	0.398616	6	15	3	5.8		12.66495861
ag03.dat	0.398471	6	15	3	6.2		12.95046043
hh02.dat	0.397494	6	15	0	9.6		16.61410868
naca1410.dat	0.397365	6	15	0	10		20.1849255
ag46c03.dat	0.397078	6	15	1	6		13.09624328
ag45ct02r.dat	0.396965	6	15	3	6.9		12.90264785
ag455ct02r.dat	0.396907	6	15	3	6.5		13.01754555
giiic.dat	0.396483	6	15	0	9.9		20.63785387
mh44.dat	0.396317	6	15	2	9.6		16.70661847
sd7003.dat	0.395984	6	15	3	8.5	1.2	17.15351248
npl9615.dat	0.395682	6	15	2	11.3		22.23923002
npl9660.dat	0.394951	6	15	2	11.3		23.18947427
defcnd3.dat	0.394314	6	15	1	11.5		15.14803011
fx69h098.dat	0.394257	6	15	1	9.9		20.73202467
ncambre.dat	0.393249	6	15	1	11.5		22.55469383
v13009.dat	0.392119	6	15	1	9		21.11584075
lg10sc.dat	0.391352	6	15	1	0		0
ames01.dat	0.391169	6	15	1	10.3		22.18069083
fx76120.dat	0.390909	6	15	1	12.1	0	28.16289896
naca23012.dat	0.390573	6	15	0	12		25.46063535
rae100.dat	0.390386	6	15	0	10		24.93279763
ht22.dat	0.390368	6	15	1	5.5		15.13183209
naca23015.dat	0.38958	6	15	0	15		31.19409281
s8025.dat	0.38784	6	15	1	8		19.64748684

Figure 8: Evaluation of Manufacturing Considerations

5.6 Final Selection



(a) sd7003 plot of CL/CD ratios with margins for changing alpha and Reynold's numbers



(b) sd7003 Profile Design

Figure 9: sd7003 Plot and Shape